

Light-intensity dependence analysis to uncover multielectron oxygen-reduction mechanism by platinum-loaded tungsten oxide

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Derivation of rate equations

Based on the assumed rate equations (3)-(9), the overall-rate equation (10) was derived assuming steady-state approximation for the short-lived intermediates as follows:

$$\langle\text{PC}\rangle(1e^-): \quad I_L\psi_0\Phi - I_L\psi_1\Phi[\langle\text{PC}\rangle(1e^-)] - k_d[\langle\text{PC}\rangle(1e^-)] = 0 \quad (\text{a})$$

$$\langle\text{PC}\rangle(2e^-): \quad I_L\psi_1\Phi[\langle\text{PC}\rangle(1e^-)] - k_r[\langle\text{PC}\rangle(2e^-)][\text{RH}] = 0 \quad (\text{b})$$

$$\text{R}\bullet: \quad k_r[\langle\text{PC}\rangle(2e^-)][\text{RH}] - k_i[\text{R}\bullet][\text{O}_2] + k_p[\text{RO}_2\bullet][\text{RH}] = 0 \quad (\text{c})$$

$$\text{RO}_2\bullet: \quad k_i[\text{R}\bullet][\text{O}_2] - k_p[\text{RO}_2\bullet][\text{RH}] - k_t[\text{RO}_2\bullet]^2 = 0 \quad (\text{d})$$

Then, these equations could be converted to:

$$\text{(a):} \quad [\langle\text{PC}(1e^-)\rangle] = I_L\psi_0\Phi / (I_L\psi_1\Phi + k_d) \quad (\text{e})$$

$$\text{(b):} \quad [\langle\text{PC}(2e^-)\rangle] = (I_L\psi_1\Phi / k_r[\text{RH}]) I_L\psi_0\Phi / (I_L\psi_1\Phi + k_d) \quad (\text{f})$$

$$\begin{aligned} \text{(c):} \quad k_i[\text{R}\bullet][\text{O}_2] &= k_r[\langle\text{PC}\rangle(2e^-)][\text{RH}] + k_p[\text{RO}_2\bullet][\text{RH}] \\ &= \frac{I_L^2\psi_0\psi_1\Phi^2}{(I_L\psi_1\Phi + k_d)} + k_p[\text{RO}_2\bullet][\text{RH}] \end{aligned} \quad (\text{g})$$

$$\begin{aligned} \text{(d):} \quad k_i[\text{R}\bullet][\text{O}_2] - k_p[\text{RO}_2\bullet][\text{RH}] &= k_t[\text{RO}_2\bullet]^2 \\ [\text{RO}_2\bullet] &= \left\{ \frac{I_L^2\psi_0\psi_1\Phi^2}{k_t(I_L\psi_1\Phi + k_d)} \right\}^{0.5} \end{aligned} \quad (\text{h})$$

The overall rate (r) of $[\text{RH}]$ consumption is:

$$r = k_r[\langle\text{PC}\rangle(2e^-)][\text{RH}] + k_p[\text{RO}_2\bullet][\text{RH}] = \frac{I_L^2\psi_0\psi_1\Phi^2}{k_t(I_L\psi_1\Phi + k_d)} + k_p[\text{RH}] \left\{ \frac{I_L^2\psi_0\psi_1\Phi^2}{k_t(I_L\psi_1\Phi + k_d)} \right\}^{0.5} \quad (\text{10})$$

The reason why a rate constant k_r is not included in the overall rate is that $\langle\text{PC}\rangle(2e^-)$ is consumed immediately after creation, i.e., the rate of creation is the same as the rate of consumption to produce $\text{R}\bullet$ without depending on k_r and $[\text{RH}]$ as described in eq. (b). In other words, assuming the complete consumption of $\langle\text{PC}\rangle(2e^-)$ means eq. (c) is shown as eq (c') without application of steady-state approximation to $[\langle\text{PC}\rangle(2e^-)]$:

$$\text{R}\bullet: \quad I_L\psi_1\Phi[\langle\text{PC}\rangle(1e^-)] - k_i[\text{R}\bullet][\text{O}_2] + k_p[\text{RO}_2\bullet][\text{RH}] = 0 \quad (\text{c}')$$