

Article

Advances in Smart Structures Using Control Algorithms for Sustainable Manufacturing

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ABSTRACT: This paper presents developments in the intelligent control of smart structures for sustainable manufacturing. This study aimed to develop advanced control approaches for the intelligent control of piezoelectric structures and suppression of oscillations. A significant achievement is the development of advanced-control algorithms. Robust control techniques, such as H-infinity control, guarantee system performance and stability in the face of uncertainties and disruptions. The addition of white noise and uncertainty to advanced finite element models is a novel aspect of this study. The outcomes of the analysis were used to present the advances made using this method. This approach is innovative because it employs intelligent control strategies that consider construction optimization by reducing the oscillations and measurement noise. By accounting for modeling uncertainty, these methods optimize construction. Optimizing smart structures makes them more sustainable and ideal for practical applications. The proposed construction is sustainable and creates an innovative design for civil and mechanical engineering applications.

Keywords: Piezoelectric structures; Intelligent control; Finite element models; Algorithms

1. Introduction

Recently, developments have been made in the use of intelligent control to reduce structural vibrations using various approaches [1–4]. The study and analysis of vibrations in constructions is extensive and of high interest to the scientific community [5]. Control is a key tool for the suppression of vibrations, contributing to the sustainability of structures [6,7] and the transition to Industry 5.0 [8]. Piezoelectric materials reduce vibrations and create modern structures that contribute to sustainable development. Several researchers have employed active control methods to reduce these vibrations. Actuators and sensors are used in active control systems to dynamically react to vibrations. Among these noteworthy developments are smart structures and materials (SMAs) [9–13]. Smart materials have created new opportunities for vibration control, including materials with piezoelectric properties that produce electric currents when subjected to mechanical stress, enabling precise vibration control [14–19]. SMAs or shape-memory alloys provide an additional means of active vibration control because they can alter their form in response to temperature variations. Self-healing materials: These materials can mitigate damage on their own,



extending the life and dependability of vibration-control systems [19–23]. Piezoelectric materials represent a new route for vibration control, which is made possible by using smart materials. These materials respond to mechanical stress by producing an electric charge, enabling precise vibration control [21–24].

Recent developments in the intelligent control of damping structural vibrations have resulted in considerable methodological and technological advances. Smart materials, including piezoelectric materials, were used in this study. Piezoelectric materials provide novel approaches for vibration control that are both accurate and long-lasting. Finite Element Analysis (FEA) [25–29] was used to assist in the development and evaluation of the control systems. To further improve sustainability, some systems can capture vibrational energy and use it in power sensors and other equipment.

Several developments have improved the structural performance and integrity of many types of real-life structures, such as high-rise buildings, bridges, and airplanes. This study highlights the use of control technologies to reduce oscillations through the application of state-of-the-art control techniques, along with the identification and addition of uncertainty to simulation models. The incorporation of modern technologies into the realm of piezoelectric materials ultimately leads to a sustainable method for building modern structures.

The research presented in this paper demonstrates the influence of control methodologies of resilient control for improving the reliability and effectiveness of intelligent structures owing to the addition of piezoelectric materials to original structures. Resilient controls based on the H-infinity (H_∞) methodology are highly effective in suppressing vibrations while maintaining stability within the system across differences in mass and stiffness. H_∞ controls have also demonstrated the ability to control wind-induced disturbances, thereby allowing stable and effective operation. The contribution of this study will affect intelligent structural controls through the development of an advanced methodology for managing the oscillations of global piezoelectric structures. The innovation of this study is that it uses advanced control techniques that consider the optimization of construction by reducing the oscillations and measurement noise. These techniques optimize construction by considering the modeling uncertainties. The construction process is optimal and sustainable. The controller has several benefits, such as remarkable disturbance rejection and resilience to noise and oscillations. It also demonstrates how improved efficiency may be attained with a lower controller order without significantly sacrificing performance. In recent years, advancements have been made in the application of intelligent controls to reduce structural vibrations using various cutting-edge technologies and techniques. Piezoelectric materials not only create modern buildings that promote sustainable growth but also reduce vibrations.

2. Methods

Intelligent structures often incorporate control systems, actuators, and sensors to enable reactions under various scenarios. Depending on how an intelligent structure is assembled and the components employed, the dynamic equations that regulate it may be complex. The smart structure consists of a cantilever beam with eight elements and four pairs. Piezoelectric patches were symmetrically linked to these elements in the bottom and top areas [21–24]. The next section provides an overview of the geometries of each intelligent structure. The dynamic characterization of the system can be expressed as follows:

$$M\ddot{q}(t) + D\dot{q}(t) + Kq(t) = f_m(t) + f_e(t) \quad (1)$$

$$q(t) = \begin{bmatrix} w_1 \\ \psi_1 \\ \vdots \\ w_n \\ \psi_n \end{bmatrix} \quad (2)$$

where K is the global stiffness matrix, f_e represents the electromechanical coupling effect (global) control force vector, and f_m is the (global) mechanical loading vector (external). Typically, sensor data are employed in feedback control systems to alter the response of a structure in real time. The major outcome is to maximize the reactivity or performance of the structure in different scenarios. where M and D represent the global mass and viscous damping matrices, respectively. Transverse deflections ψ_i and rotations [25–29], where n represents the finite elements (total number), were used in the analysis. The vectors (upward) f_m and w have values greater than zero. The independent variable $q(t)$ is defined by the rotations ψ_i and transverse deflections w_i as follows:

$$x(t) = \begin{bmatrix} q(t) \\ \dot{q}(t) \end{bmatrix} \tag{3}$$

$f_e(t)$ can be defined as $Bu(t)$ by expressing it using the formula $F_e^* \cdot u$, where u is the actuator voltage, and the piezoelectric force is expressed using the formula F_e^* ($2n \times n$) for a unit created on the actuator [30,31]. Therefore, the disturbance vector is expressed as $d(t) = f_m(t)$. Next,

$$\begin{aligned} \dot{x}(t) &= \begin{bmatrix} 0_{2n \times 2n} & I_{2n \times 2n} \\ -M^{-1}K & -M^{-1}K \end{bmatrix} x(t) + \begin{bmatrix} 0_{2n \times n} \\ M^{-1}F_e^* \end{bmatrix} u(t) + \begin{bmatrix} 0_{2n \times 2n} \\ M^{-1} \end{bmatrix} d(t) \\ &= Ax(t) + Bu(t) + Gd(t) \\ &= Ax(t) + [B \quad G] \begin{bmatrix} u(t) \\ d(t) \end{bmatrix} \\ &= Ax(t) + B\tilde{u}(t) \end{aligned} \tag{4}$$

The units used were meters (m), radians (rad), seconds (s), and Newtons (N). The proposed method maintains stability in the time domain. Furthermore, in the frequency domain, the following formula is implemented for a more thorough examination of stability [21–23]:

$$y(t) = [x_1(t) \times x_3(t) \times \dots \times x_{n-1}(t)]^T = C \times x(t) \tag{5}$$

The first-order dynamics of the smart structure are captured using this state-space representation, where the state vector $x(t)$ comprises both the velocity and displacement. The uncertainty in the M and K matrices was addressed using the following method:

$$\begin{aligned} K &= K_0(I + kpI_{2n \times 2n}\delta_K) \\ M &= M_0(I + mpI_{2n \times 2n}\delta_M) \end{aligned} \tag{6}$$

Moreover, given that, $D = 0.0005(K + M)$, one appropriate form for D is,

$$\begin{aligned} D &= 0.0005[K_0(I + kpI_{2n \times 2n}\delta_K) + M_0(I + mpI_{2n \times 2n}\delta_M)] = \\ &D_0 + 0.0005[K_0kpI_{2n \times 2n}\delta_K + M_0mpI_{2n \times 2n}\delta_M] \end{aligned} \tag{7}$$

However, given that in general:

$$D = \alpha \times K + \beta \times M$$

Matrix D , which represents structural damping, can be simplified by considering it (following Rayleigh damping) as a linear combination of stiffness and mass. In this situation, the first and second normal vibration modes yielded values of α and β , which were determined to be 0.0005. In the same way as K and M , D can be expressed as

$$D = D_0(I + dpI_{2n \times 2n}\delta_D) \tag{8}$$

The uncertainty was incorporated by adding a proportional deviation to the pertinent matrices. Herein, this uncertainty equation works well because the length is a perfectly measured quantity. Compared with the major matrices, the terms were more likely to cause uncertainty. Again, it was assumed that

$$\|\Delta\|_{\infty} \stackrel{\text{def}}{=} \left\| \begin{bmatrix} I_{n \times n} \delta_K & 0_{n \times n} \\ 0_{n \times n} & I_{n \times n} \delta_M \end{bmatrix} \right\|_{\infty} < 1 \tag{9}$$

Therefore, zero subscript denotes nominal values, and k_p and m_p are used to adjust the proportion value. It is recommended that the norm for matrix $A_{n \times m}$ be ascertained through

$$\|A\|_{\infty} = \max_{1 \leq j \leq m} \sum_{i=1}^n |a_{ij}|$$

When these conditions are considered, Equation (4) becomes,

$$\begin{aligned} M_0 \left(I + m_p I_{2n \times 2n} \delta_M \ddot{q}(t) \right) + K_0 \left(I + k_p I_{2n \times 2n} \delta_K q(t) \right) + 0.0005 [K_0 k_p I_{2 \times 2} \delta_K + M_0 m_p I_{2 \times 2} \delta_M] \dot{q}(t) + f_m(t) + f_e(t) \\ \Rightarrow M_0 \ddot{q}(t) + D_0 \dot{q}(t) + K_0 q(t) = - [M_0 m_p I_{2n \times 2n} \delta_M \ddot{q}(t) + 0.0005 [K_0 k_p I_{2 \times 2} \delta_K + M_0 m_p I_{2 \times 2} \delta_M] \dot{q}(t) + \\ K_0 k_p I_{2n \times 2n} \delta_K q(t)] + f_m(t) + f_e(t) \\ \Rightarrow M_0 \ddot{q}(t) + D_0 \dot{q}(t) + K_0 q(t) = \tilde{D} q_u(t) + f_m(t) + f_e(t) \end{aligned} \tag{10}$$

where,

$$q_u(t) = \begin{bmatrix} \ddot{q}(t) \\ \dot{q}(t) \\ q(t) \end{bmatrix} \tag{11}$$

$$\begin{aligned} \tilde{D} &= - [M_0 m_p \quad K_0 k_p] \begin{bmatrix} I_{2n \times 2n} \delta_M & 0_{2n \times 2n} \\ 0_{2n \times 2n} & I_{2n \times 2n} \delta_K \end{bmatrix} \begin{bmatrix} I_{2n \times 2n} & 0.0005 I_{2n \times 2n} & 0_{2n \times 2n} \\ 0_{2n \times 2n} & 0.0005 I_{2n \times 2n} & I_{2n \times 2n} \end{bmatrix} \\ &= G_1 \cdot \Delta \cdot G_2 \end{aligned}$$

Expressing Equation (7) in state space form results in,

$$\begin{aligned} \dot{x}(t) &= \begin{bmatrix} 0_{2n \times 2n} & I_{2n \times 2n} \\ -M^{-1}K & -M^{-1}D \end{bmatrix} x(t) + \begin{bmatrix} 0_{2n \times n} \\ M^{-1}f_e \end{bmatrix} u(t) + \begin{bmatrix} 0_{2n \times 2n} \\ M^{-1} \end{bmatrix} d(t) + \begin{bmatrix} 0_{2n \times 6n} \\ M^{-1}G_1 \cdot \Delta \cdot G_2 \end{bmatrix} q_u(t) \\ &= Ax(t) + Bu(t) + Gd(t) + G_u G_2 q_u(t) \end{aligned} \tag{12}$$

In the proposed method, the uncertainty of the original matrices is considered an additional measure of uncertainty. These equations capture the concept of dynamic loads or changing conditions being responded to by smart structures through active and flexible control. It is difficult to create control system algorithms that effectively confront the status of the structure and simultaneously address external forces (Figure 1).

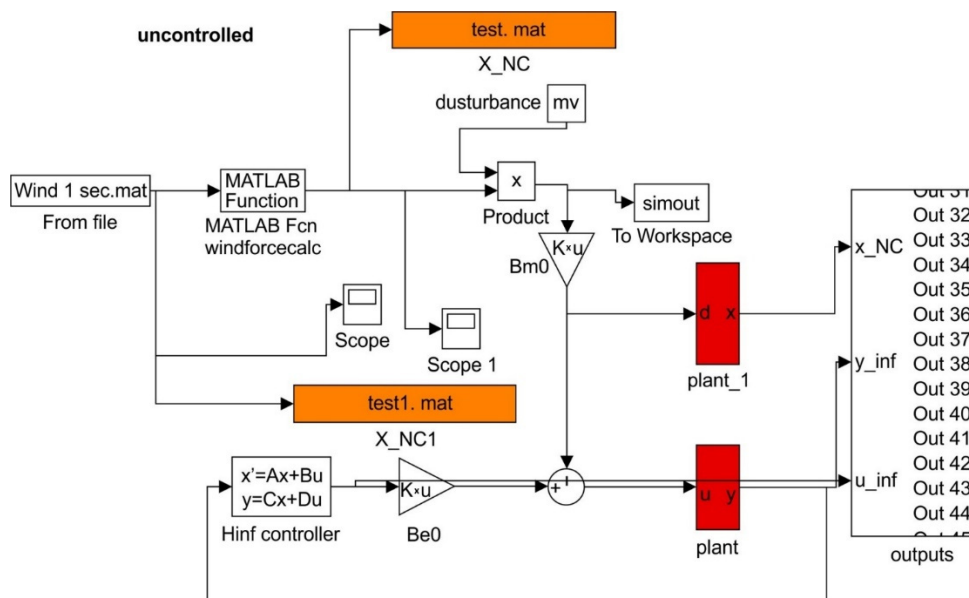


Figure 1. The results of the simulation. Only indicative outputs are presented.

3. Results

The cantilever smart structure (Figure 2) studied in this section features four pairs of symmetrically bonded piezoelectric patches. These were placed at the bottom and top of each beam element. The beam details are presented in Table 1.

Table 1. Features of the smart beam.

Parameters	Values
Wp, pzt Width,	0.003 m
W, for Width of the beam	0.003 m
L, for beam length	1.40 m
hp, piezoelectric thickness	0.0002 m
h, for the thickness of the beam	0.096 m
ρ , for Beam density	1800 kg/m ³
E, for the beam's stiffness (Young's modulus)	1.7×10^{11} N/m ²
Ep, pzt Young's modulus	6.3×10^{10} N/m ²
d ₃₁ the Piezoelectric constant	250×10^{-12} m/V
bs, ba, thickness of Pzt	0.002 m

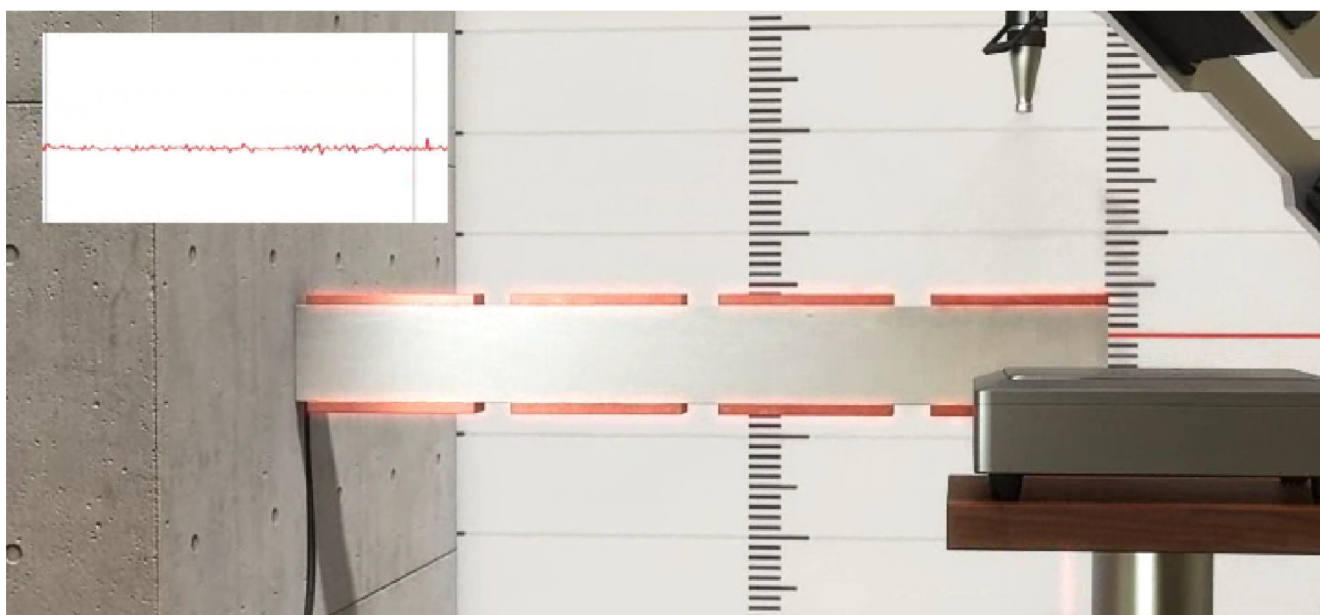


Figure 2. Smart structure.

Subheadings may be used to structure this section. It should offer a succinct and precise explanation of the experimental findings, their meanings, and any inferred experimental inferences. First, the nominal performance was created on the MATLAB software platform (v.6.5, MathWorks, Natick, MA, USA) (Figures 3 and 4).

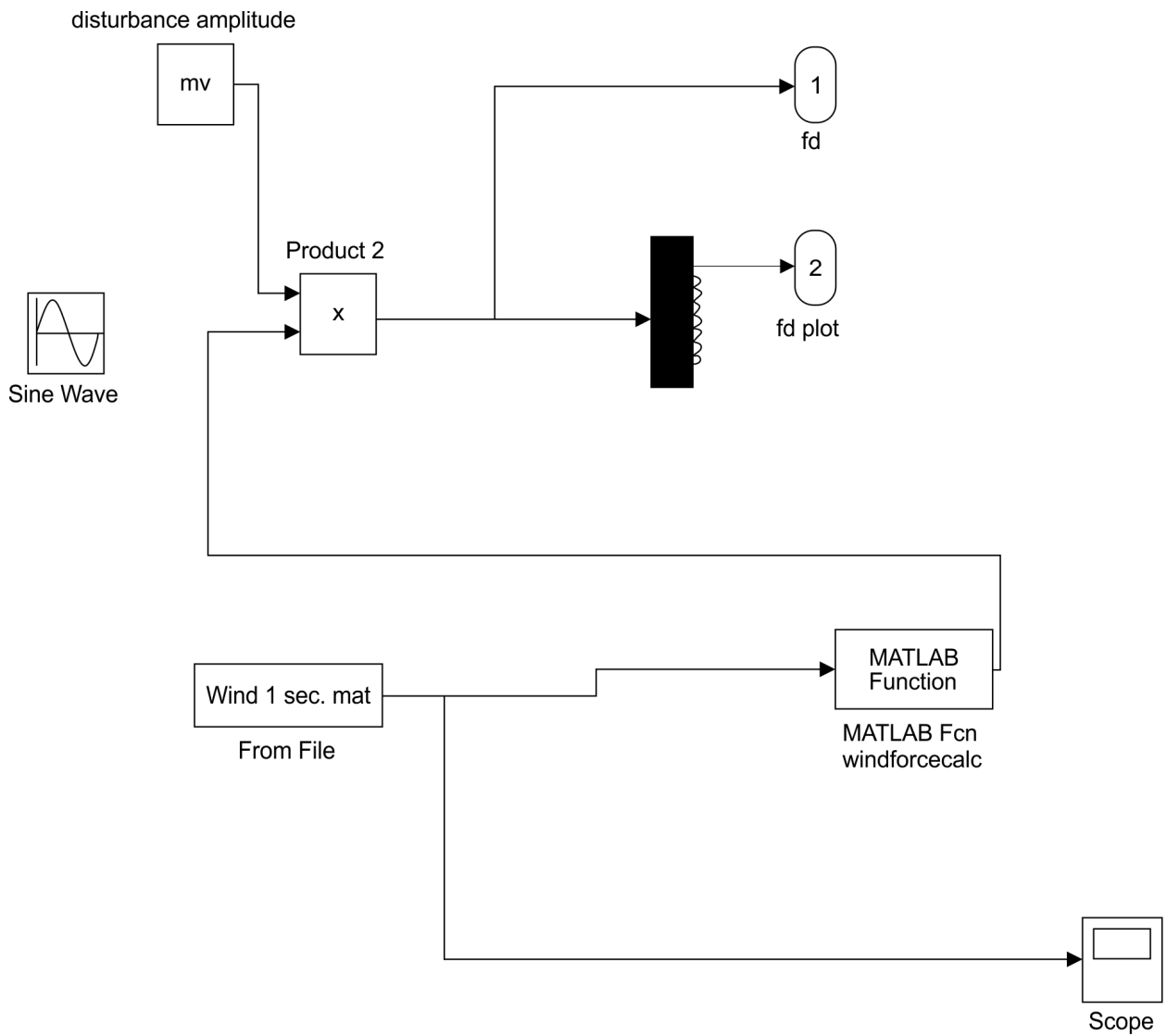


Figure 3. The Simulink diagram.

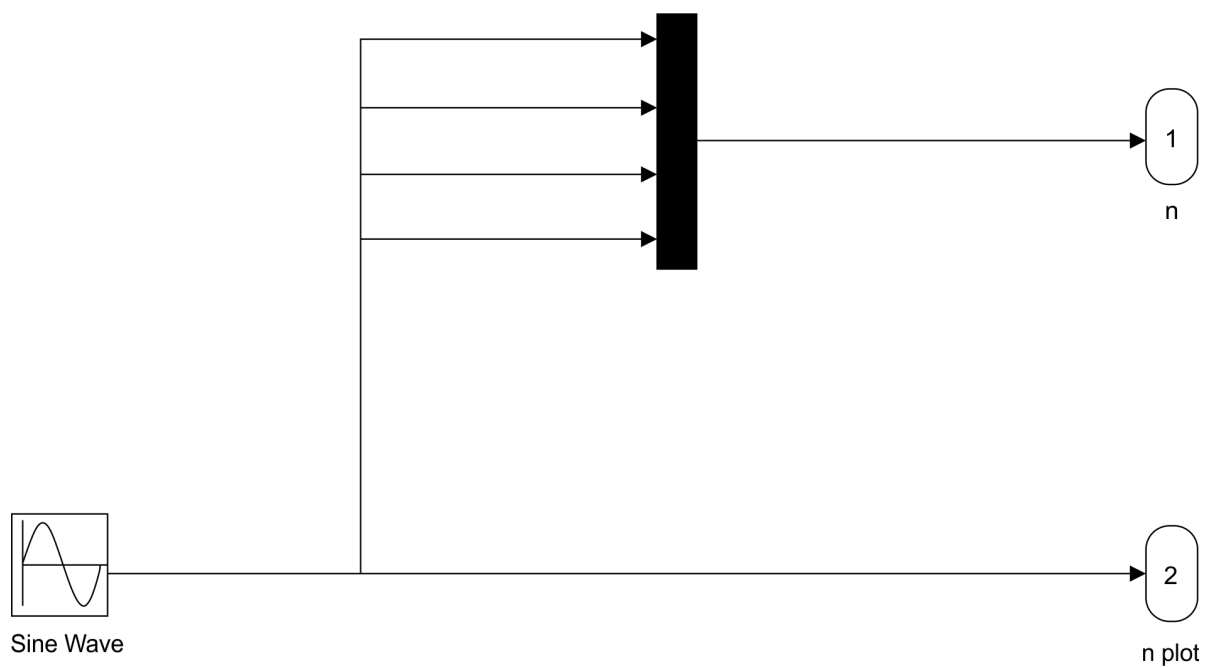


Figure 4. The sinusoidal Force in Simulink.

Next, uncertainty modeling was performed using Equations (6)–(12), and the developed MATLAB code was applied to the data.

In the context of the results, the disturbance being a sinusoidal force suggests that the system is subjected to a periodic input, and the H_∞ control is used to stabilize and optimize the system performance under this disturbance. To break down the description of the results and what Figure 5 represents, in the left diagram, matrices A and B (from Equation (12)) are analyzed with H_∞ Control. Figure 5 illustrates the response of the system, focusing on the different elements of matrices A and B from Equation (12), which are likely to be parts of the state-space representation of the system. These matrices represent the system dynamics and control input relationships. H_∞ Control Application: The left diagram shows the system behavior when H_∞ control is applied to specific elements of matrices A and B. The middle diagram shows a system behavior comparison with and without the application of the control, and the (blue curve) depicts the results when the H_∞ controller was applied. This line shows the response of the system when the robust controller is active, thereby demonstrating improved stability and reduced oscillations.

Without Control (Open-Loop System–Various Colors): The other lines in different colors represent the system response without control (open-loop). These uncontrolled responses are likely to be oscillatory or unstable, demonstrating the effect of sinusoidal disturbances on the system when corrective measures are not implemented in the control system.

The right-hand diagram illustrates the control voltages generated by the H_∞ controller for the different outcomes of matrices A and B. These control voltages represent the control inputs (likely voltages applied to actuators or smart materials) required by the H_∞ controller to stabilize the system in the presence of a given disturbance.

B was tested to observe the change in control effort (in terms of voltage). The goal is to ensure that the controller maintains stability and performance across different configurations of system dynamics (variations with A and B: different values or combinations of A and B).

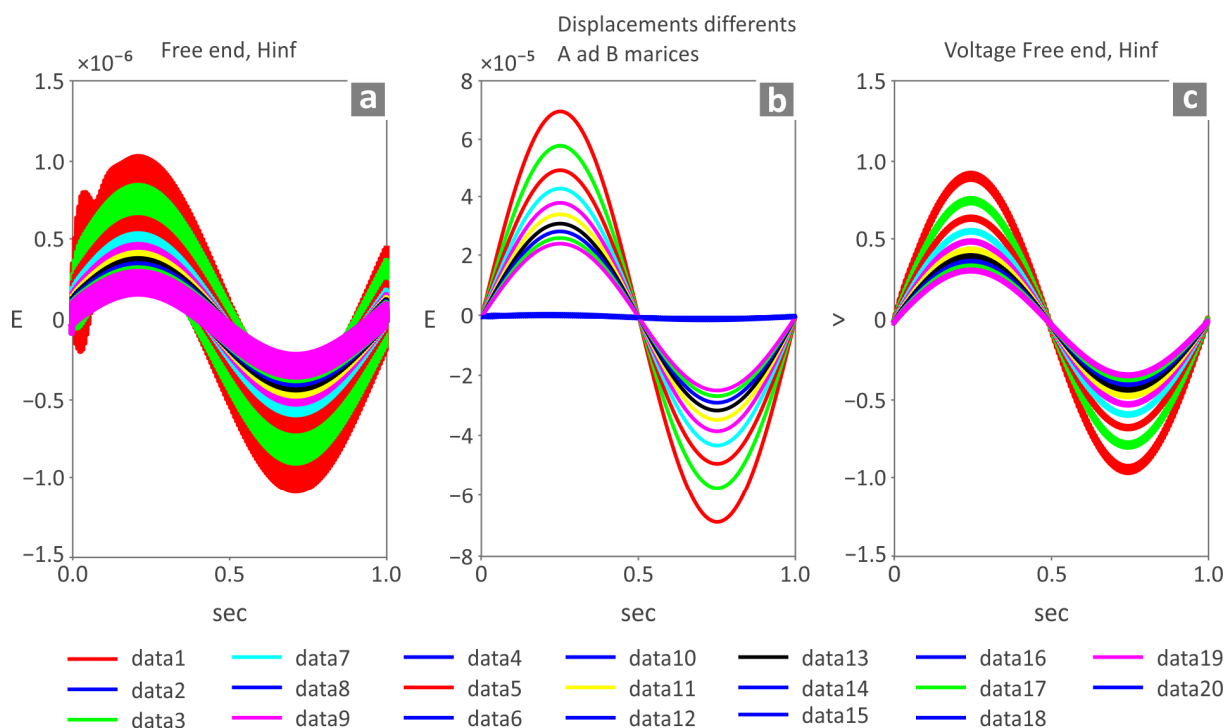


Figure 5. (a) Displacements with Hinf with different prices A and B, (b) Displacements without and with control with different values A, B, (c) Control Voltages with Hinf with different prices A and B.

UNCERTAINTY Modeling

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% uncertainty modeling
delta_m = 10-5;
delta_k = delta_m2;
% delta_d = delta_m;
% Delta = eye(3 × nd);
X_m = mm1 × delta_m;
X_k = kk1 × delta_k;
X_d = 0.0005 × (X_m + X_k);

G_bar = -[X_m X_d X_k];
P_m = eye(nd);
P_k = eye(nd);
P_d = eye(nd);

G_bar0 = [zeros(nd, 3 × nd);
invM × G_bar];
E1 = [ P_m          zeros(nd, nd);
zeros(nd, nd)      P_d;
zeros(nd, 2 × nd)];

E2 = [zeros(nd, 2 × nd)
zeros(nd, 2 × nd)
zeros(nd, nd) P_k];

% from d, n, p to uncertainty
Sdq = (E1 + E2 × H)*(eye(2 × nd) - B0 × K × C0 × H)-1 × G0 × Wd;
Snq = (E1 + E2 × H)*(eye(2 × nd) - B0 × K × C0 × H)-1 × B0 × K × Wn;
Spq = (E1 + E2 × H)*(eye(2 × nd) - B0 × K × C0 × H)-1 × G_bar0;
Spe = We × J × H × (eye(2 × nd) + B0 × (K × (eye(nd/2) - C0 × H × B0 × K)-1 × C0 × H))
× G_bar0;
Spu = Wu × K × (eye(nd/2) - C0 × H × B0 × K)-1 × C0 × H × G_bar0;
Sde = We × J × H × (eye(2 × nd) + B0 × (K × (eye(nd/2) - C0 × H × B0 × K)-1 × C0 × H)) ×
G0 × Wd;
Sne = We × J × H × B0 × K × (eye(nd/2) - C0 × H × B0 × K)-1 × Wn;
Sdu = Wu × K × (eye(nd/2) - C0 × H × B0 × K)-1 × C0 × H × G0 × Wd;
Snu = Wu × K × (eye(nd/2) - C0 × H × B0 × K)-1 × Wn;

M = [Spq Sdq Snq;
Spe Sde Sne; mass and stiffness matrices
Spu Sdu Snu];

```

Figure 5 shows a detailed analysis of the outcome of the smart system for sinusoidal disturbances with and without control. The H_∞ controller significantly enhanced the robustness of the system by reducing oscillations and stabilizing the dynamic response, as illustrated in the middle diagram.

The mass (M) and stiffness (K) matrices from Equation (12) are the main focus of the H_∞ control analysis of the system reaction to wind force disturbances, as shown in Figure 6. Under H_∞ control, the graph on the left illustrates how the displacements change for various portions of the mass (M) and stiffness (K) matrices. This demonstrates how well the control handles these fluctuations, reduces the displacements, and stabilizes the system.

The displacements with and without control are compared in the central diagram. The system with H_∞ control is indicated by the blue line, which indicates increased stability and fewer vibrations. The larger displacements of the colored lines (open-loop and no-control) highlight the effectiveness of the control in reducing the influence of wind disturbance.

The control voltages for various mass and stiffness levels are shown on the right side of the diagram. The voltages indicate the required amount of control for the system. The voltages indicate the amount of control that must be used to keep the objects stable under these changing circumstances. The findings demonstrate that the system maintains stability with minimal vibration in various configurations and that the control effort is tolerable. H_∞ control, even with different masses and stiffnesses, often significantly minimizes vibrations and maintains stability. These results attest to the efficiency of the windbreaks in controlling wind disturbances.

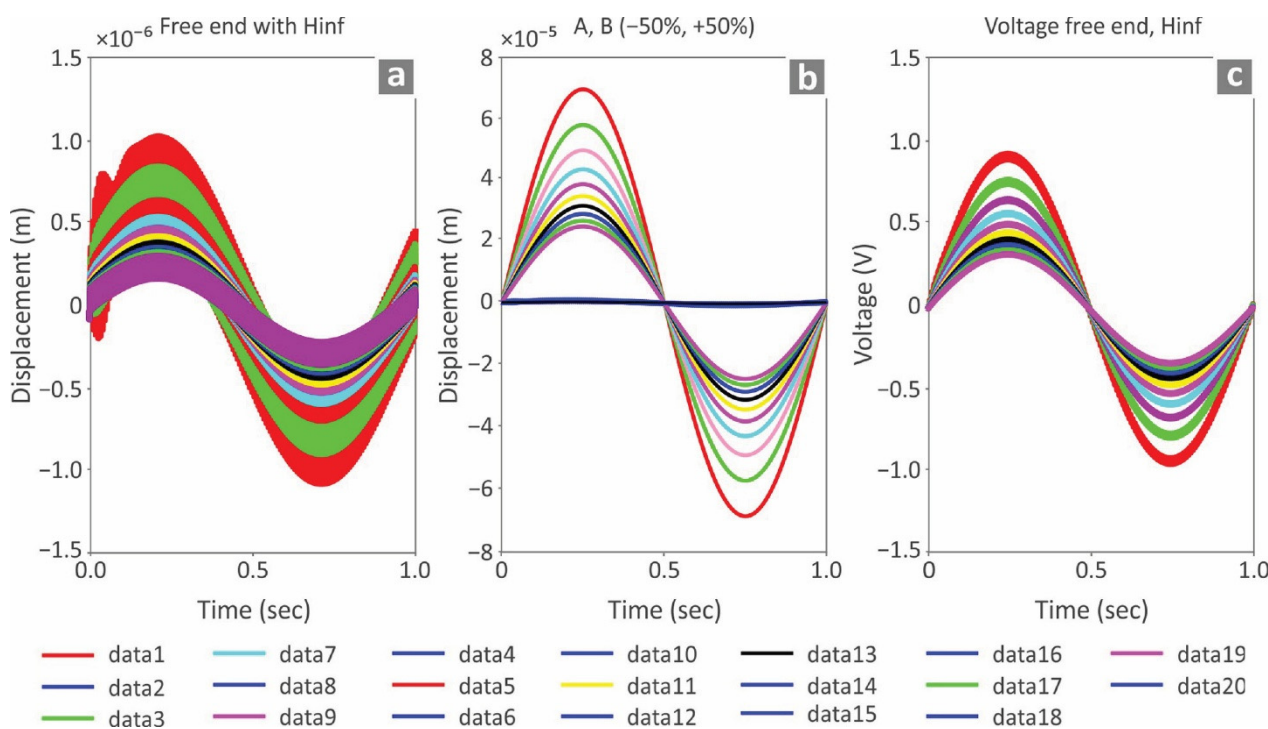


Figure 6. (a) Displacements with H infinity with different prices M and K, (b) Displacements with and without application of control with variable prices M, K, (c) Control Voltages with H infinity with variable prices M and K.

Regarding the subsequent collection of outcomes, where the disturbance is a wind force, Figure 7 offers insights into the system response under this new disturbance. The details of each section are presented in the figure. Left Diagram: Displacements for different elements belonging to matrices A and B (Equation (12)) with H_∞ control. Figure 6 illustrates the displacements of the system for various elements of matrices A and B (which are part of the state-space equation representation in Equation (12)) under the influence of H_∞ control. This refers to the extent to which the nodes in the smart structure (e.g., a smart beam) are displaced as a result of wind force disturbance. H_∞ Control Impact: The left diagram shows how H_∞ control manages the displacements of the different components for matrices A and B.

Middle Diagram: Displacements with and Without Control (open-loop versus closed-loop). The middle diagram in Figure 7 focuses on a comparison of displacements with and without control: With H_∞ Control (Blue Line): The blue line represents the system’s displacements when H_∞ control is applied. Here, the control system actively reduces the displacement caused by the wind force, leading to a more stable and predictable behavior.

Without Control (Open-Loop, Different Colors): Colored lines represent the system’s behavior without control (open-loop scenario). These lines likely show larger displacements or oscillatory behavior owing to wind disturbances, indicating a lack of stability and robustness in the open-loop system. Key Insight: This comparison demonstrates the efficiency of the H_∞ control in reducing wind-induced displacements, clearly showing improved performance (less displacement) when the control is active compared with the open-loop case—right Diagram: Control Voltages with H_∞ for different A and B values in the rightmost diagram. Figure 7 shows the control voltages required by the H_∞ controller to maintain stability for varying values of matrices A and B. These voltages represent the inputs (possibly the voltages applied to the actuators or other control mechanisms) necessary to stabilize the system under wind-force disturbances.

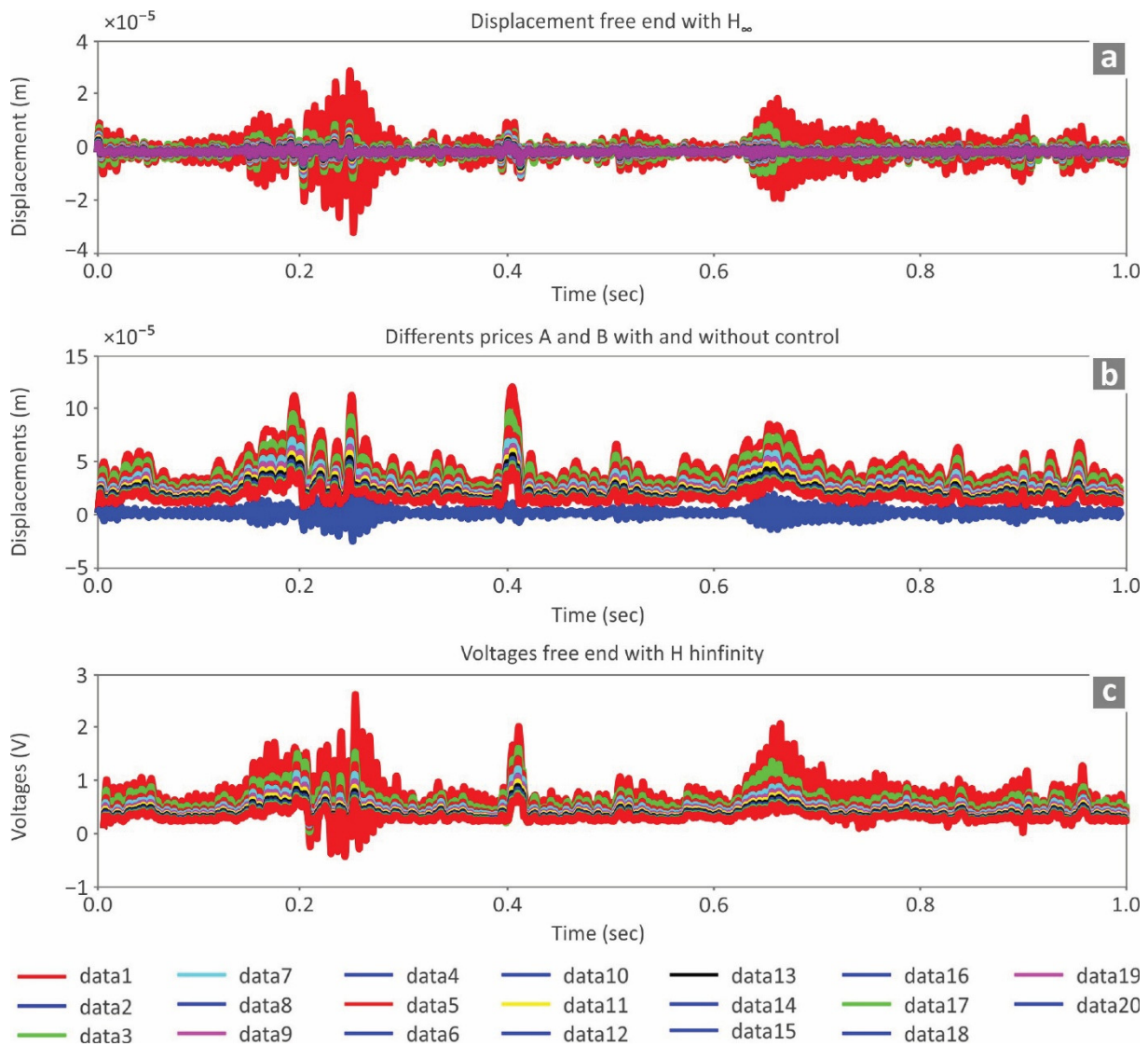


Figure 7. Wind force: (a) Displacements with H-infinity with different prices A and B, (b) Displacements with and without control with different prices A, B, (c) Control Voltages with Hinfinity with different prices A and B.

In Figure 8, the system response to the wind force disturbance is analyzed using H_∞ control, focusing on the mass (M) and stiffness (K) matrices from Equation (12). The diagram on the left shows how the displacements vary for discrete parts of the stiffness and mass matrices under the H_∞ control. The graphs above show that when the control method (H-infinity) was implemented, the system showed an increase in stability as well as a decrease in displacements owing to the control of the vibrations caused by the disturbance (wind). The graph on the left shows two lines: one with the application of control (blue) and one without (red). The blue line shows a smaller displacement compared to the red line, which has a larger displacement. There was a clear risk that applying the control would give an unstable result, as measured in a comparison of the response magnitudes of the systems with and without control due to the disturbance (wind). However, based on the results from simulations with varying stiffness and mass values of the system, the graph on the right shows the control voltages required to keep the system stable. The amount of control required to achieve the response was very low, and the system was able to remain stable with very little vibration across all configurations tested.

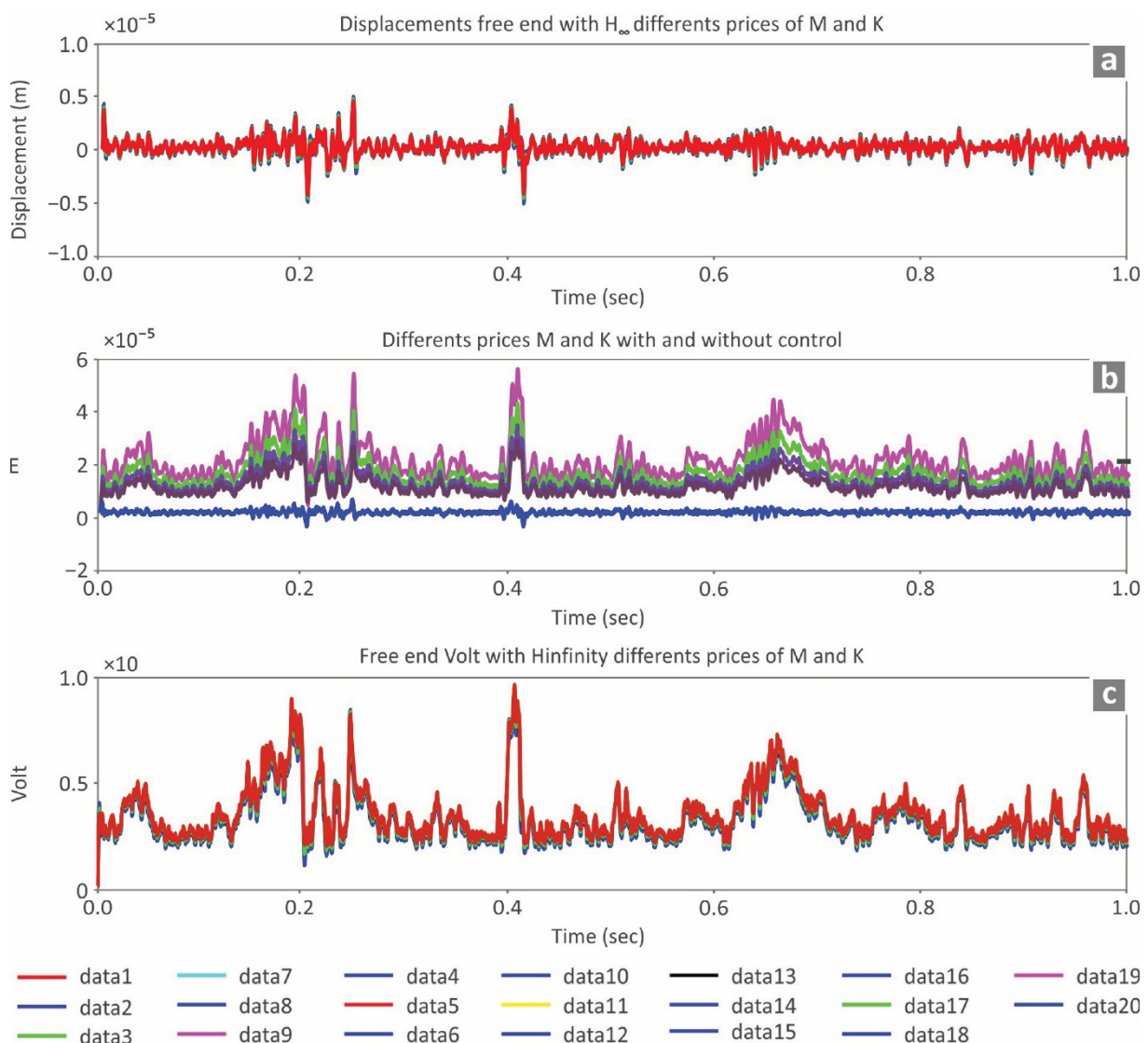


Figure 8. Wind force: (a) Displacements with Hinfinitiy with different prices M, K, (b) Displacements with and without application of control with different values for M, K, (c) Control Voltages with Hinfinitiy with different prices M and K.

In conclusion, the H-infinity controller is a viable means of stabilizing the system and significantly reducing the amount of displacement experienced during a disturbance (*i.e.*, wind). To validate the time-

domain results, plots of both the closed- and open-loop systems for the frequency-frequency view were created, as shown in Figure 9. The singular value of the system was calculated as the effect of a disturbance, that is, the error. The influence of An was monitored. In particular, a significant improvement in perturbation inaccuracy was observed up to a frequency of 1000 Hz.

Reducing vibrations is a fundamental problem for engineers, and creating sustainably optimized structures is important. In conclusion, this study achieves the following:

1. Complete suppression of the oscillations. With the control, E was reduced from almost 6.0×10^{-5} to less than 0.5×10^{-5} , while the displacement in meters was reduced from almost 10^{-4} to less than 3.0×10^{-5} .
2. Introduction of uncertainty in the simulation model.
3. Application of advanced control techniques to smart structures.
4. Creation of optimal and sustainable structures.
5. Control of structures in both the time and frequency domains.
6. Modeling of the structure through algorithms and the introduction of dynamic loads.
7. The results for various types of dynamic loads were examined, considering noise and modeling errors.

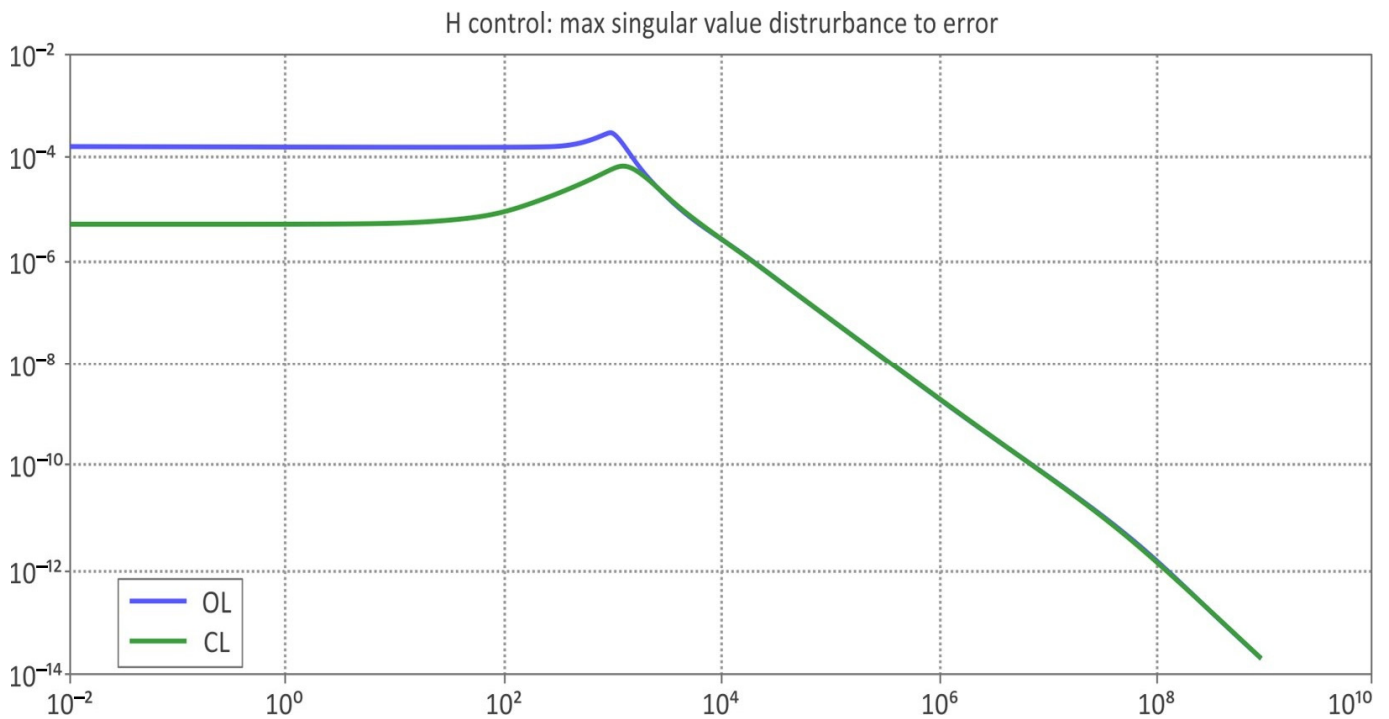


Figure 9. Frequency domain open and closed loop, max singular value.

4. Discussion

This study presents advances in the intelligent control of sustainable structures. The goal of this study is to create sophisticated control strategies to suppress oscillations and intelligently regulate the piezoelectric structures. The creation of sophisticated control algorithms is a significant accomplishment. The development of Adaptive Control Techniques has been made possible by the time-varying characteristics of piezoelectric materials [10,32,33]. This study provides insight into the development of methods to reduce oscillations caused by variations in mass and stiffness (matrix stiffness) arising from various modeling methods and/or structural damage that may result from varying the initial conditions of the system. Two control strategies were used to suppress the oscillations caused by variations in the initial conditions of the system. Both exhibited robust performances, meaning that despite facing unexpected conditions (uncertainties and structural anomalies), re-stabilization and suppression of oscillations were achieved.

Because piezoelectric materials were added to the original structures, the study reported in this paper shows how resilient control techniques can improve the dependability and efficiency of intelligent structures. It has been demonstrated that resilient controls based on the H-infinity (H_∞) technique are very successful in suppressing vibrations while preserving system stability over variations in mass and stiffness. Additionally, H_∞ controllers can manage wind-induced disruptions, enabling steady and efficient operation. The development of a sophisticated technique for controlling the oscillations of global piezoelectric structures will impact intelligent structural control.

Although the control methods described will change how the initial conditions are defined for a system, the proposed methods are capable of effectively minimizing oscillations and thereby producing stable motion. A significant characteristic of the results presented in this section is their robustness to variations in parameter values, which demonstrates that the proposed methods can maintain the controllability and stability of the system for a much wider range of initial conditions than when these methods are not used. The ability to create damping in the oscillation response of the system to varying initial conditions is a critical aspect of the reliability and robustness of the system, ensuring that it functions according to its intended performance level. Furthermore, given the potential for a number of uncertainties and modeling errors to occur in real-world applications, the evidence provided by the results presented in this study provides valuable insights into the potential implications of these uncertainties on the long-term performance and operational viability of the system, as described.

The controller offers numerous advantages: the system exhibits exceptional disturbance rejection and is robust in the presence of noise and oscillations. Furthermore, it illustrates how a reduced controller order can achieve enhanced efficiency without substantially compromising the performance. The use of intelligent controls to reduce structural vibrations by employing various state-of-the-art technologies and methods has advanced in recent years. In addition to producing contemporary structures that support sustainable growth, piezoelectric materials can reduce vibrations. To reduce vibrations, several researchers have employed active control techniques. Active control systems employ sensors and actuators to respond to vibrations dynamically. The creation of Smart Structures and Materials is a significant advancement in this field.

5. Conclusions

In conclusion, this study presents innovations in the modeling of new sustainable structures that use new modern materials and smart systems. These structures, in order to operate, use advanced control techniques developed analytically in this study. The features of this study illustrate a reduction in oscillations through the recording of stiffness. This indicates deviations from the initial conditions of the system, which may be indicative of modeling errors or structural damage. This is perceptually configured with the damping of oscillations under variable initial conditions. This study recommends employing robust and operational modeling for system design analysis. Intelligent structures that utilize piezoelectric materials must possess disturbance rejection properties. The capability to design a system with disturbance rejection properties and data logging capabilities using a reliable and accurate version of MATLAB proved to be a valuable platform for modeling and simulating intelligent systems. The state-space simulation employed in this study was designed to develop and implement an H-infinity controller to compare the advantageous attributes of resilient control using disturbance variable recordings, as exemplified in the preceding chapters. Innovations in the modeling of new sustainable structures that use smart materials and intelligent structures are presented in this study. These structures employ robust control strategies that are theoretically defined in this study in order to function. The controller has several benefits, such as the remarkable rejection of disturbances and resilience to oscillations and noise. It also shows how improved efficiency may be attained with a lower controller order without significantly sacrificing the performance. In recent years, advancements have been made in the application of intelligent controls to reduce structural vibrations using various cutting-edge technologies and techniques. Piezoelectric materials can not only

create modern buildings that promote sustainable growth but also reduce vibrations. The innovation of this study is that it uses advanced control techniques that consider the optimization of construction by reducing oscillations and measurement noise. These techniques optimize construction by considering modeling uncertainties. The construction process becomes optimal and sustainable.

Author Contributions

A.M. and M.P.: software, formal analysis, writing review, and editing; G.E.S.: methodology; A.P.: investigation and software; N.V.: validation. All authors have read and agreed to the published version of this manuscript.

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Not applicable.

Informed Consent Statement

Not applicable.

Data Availability Statement

The authors confirm that the data supporting the findings of this study are available in this article.

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Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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